



Radar Systems Engineering Lecture 9 Antennas

Part 2 - Electronic Scanning and Hybrid Techniques

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Block Diagram of Radar System





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Search Radar Equation

Track

S / N = $\frac{P_t G^2 \lambda^2 \sigma}{(4 \pi)^3 R^4 k T_s B_n L}$ Radar This A_e = Effective Area Equation Lecture T_s = System Noise Radar Temperature S/N = $\frac{P_{av} A_e t_s \sigma}{4 \pi \Omega R^4 k T_s L}$ Equation Lecture

G = Gain

L = Losses

* IEEE Standard Definitions of Terms for Antennas (IEEE STD 145-1983)

in others Designed for optimum gain (directivity) and minimum loss of energy during transmit or receive

Direct microwave radiation in desired directions, suppress

- A radiated electromagnetic wave consists of electric and magnetic fields which jointly satisfy Maxwell's Equations
- "Means for radiating or receiving radio waves"*







Radar Antennas Come in Many Sizes and Shapes





Mechanical Scanning Antenna



Electronic Scanning Antenna

Hybrid Mechanical and Frequency Scanning Antenna

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Multiple antennas combined to enhance radiation and shape pattern



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Want fields to interfere constructively (add) in desired directions, and interfere destructively (cancel) in the remaining space



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- Geometrical configuration
 - Linear, rectangular, triangular, etc
- Number of elements N
- Element separation **D**
- Excitation phase shifts ϕ_n
- Excitation amplitudes a_n
- Pattern of individual elements
 - Dipole, monopole, etc.

Array Factor Antenna Element





• The "Array Factor" AF, is the normalized radiation pattern of an array of isotropic point-source elements

$$\mathbf{AF}(\theta,\phi) = \sum_{n=1}^{N} \mathbf{a}_{n} \, \mathbf{e}^{\mathbf{j}\phi_{n}} \mathbf{e}^{\mathbf{j}\mathbf{k}\cdot\vec{r}_{n}\cdot\hat{r}}$$



Source Element n:

Excitation

$$a_n e^{j\Phi_n}$$

Position Vector $\vec{r}_1 = \hat{x} x_n + \hat{y} y_n + \hat{z} z_n$

Observation Angles (θ,φ):

Observation Vector

 $\hat{\mathbf{r}} = x\sin\theta\cos\phi + \hat{y}\sin\theta\sin\phi + \hat{z}\,\cos\theta$

Free-Space Propagation Constant $k = \frac{2\pi}{\lambda} = \frac{2\pi f}{c}$











- Major lobes and sidelobes
 - Mainlobe narrows as N increases
 - No. of sidelobes increases as N increases
 - Width of major lobe = $2\pi/N$
 - Height of sidelobes decreases as N increases
- Changing β will steer the peak of the beam to a desired $\theta = \theta_0$
 - Beam direction varies from 0 to $\,\pi$
 - ψ varies from kd + β to kd + β
- Condition for no grating lobes being visible:

$$\frac{\mathrm{d}}{\lambda} < \frac{1}{1 + \left|\cos\theta_{\mathrm{o}}\right|}$$

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\theta_{o} = angle off broadside
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Note how $\boldsymbol{\theta} \,$ is defined.



Array and Element Factors









The Overall Array Gain is the Product of the Element Gain and the Array Factor Gain

| Array | | Element | | Array Factor |
|-------|---|---------|---|--------------|
| Gain | = | Gain | + | Gain |
| (dBi) | | (dBi) | | (dBi) |

Array
Factor
$$G_{AF}(\theta,\phi) = \frac{4\pi |AF(\theta,\phi)|^2}{P_{RAD}}$$

$$\mathbf{P}_{\mathbf{RAD}} = \int_{0}^{2\pi} \int_{0}^{\pi} \left| \mathbf{AF}(\theta, \phi) \right|^{2} \sin \theta \, d\theta \, d\phi$$

Individual Array Elements are Assumed to Be Isolated





- Student Problem:
 - Calculate the normalized array factor for an array of 3 isotropic radiating elements. They are located along the x-axis (center one at the origin) and spaced $\lambda/2$ apart. Relevant information is 2 and 3 viewgraphs back.
 - Use the results of this calculation and the information in viewgraph 28 of "Antennas Part 1' to calculate the radiation pattern of a linear array of three dipole, $\lambda/2$ apart on the x-axis.



Increasing Array Size by Adding Elements







Increasing Broadside Array Size by **Separating Elements**





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Ordinary Endfire Uniform Linear Array





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Linear Phased Array Scanned every 30 deg, N = 20, d = $\lambda/4$





 $k_o = 2\pi f_o / c$ separation d < $\lambda / 2$

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$$k_o = 2\pi c/f_o$$

 $\psi = k_o d\cos\theta_o + \beta = 0$

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$$\mathbf{AF}_{n}(\theta,\phi) = \left\{ \frac{1}{M} \frac{\sin\left(\frac{M\psi_{x}}{2}\right)}{\sin\left(\frac{\psi_{x}}{2}\right)} \right\} \left\{ \frac{1}{N} \frac{\sin\left(\frac{N\psi_{y}}{2}\right)}{\sin\left(\frac{\psi_{y}}{2}\right)} \right\}$$

where $\psi_x = \mathbf{k} \mathbf{d}_x \sin \theta \cos \phi + \beta_x$ $\psi_y = \mathbf{k} \mathbf{d}_y \sin \theta \sin \phi + \beta_y$

Progressive phase to scan to (θ_o, ϕ_o) : $\beta_x = -kd_x \sin \theta_o \cos \phi_o$

 $\beta_{\rm y} = -\mathbf{k}\mathbf{d}_{\rm y}\sin\theta_{\rm o}\sin\phi_{\rm o}$

Figure by MIT OCW.

• To scan over all space without grating lobes: $d_x < \lambda / 2$ and $d_y < \lambda / 2$

- The array beamwidth in the plane of scan increases as the beam is scanned off the broadside direction.
 - The beamwidth is approximately proportional to $1/\cos\theta_0$
 - where θ_o is the scan angle off broadside of the array
- The half power beamwidth for uniform illumination is:

$$\theta_{\rm B} \approx \frac{0.886\lambda}{\rm Nd\cos\theta_o}$$

• With a cosine on a pedestal illumination of the form:

 $\mathbf{A} = \mathbf{a}_{0} + 2\mathbf{a}_{1}\cos(2\pi n/N)$

And the corresponding beamwidth is:

$$\theta_{\rm B} \approx \frac{0.886\lambda}{\rm N\,d\,\cos\theta_o} \left[1 + 0.636(2a_1/a_0)\right]$$

 In addition to the changes in the main beam, the sidelobes also change in appearance and position.

- Time delay steering requires:
 - Switched lines
- It is a relatively lossy method
- High Cost
- Phase shifting mainly used in phased array radars

Adapted from Skolnik, Reference 1 IEEE New Hampshire Section IEEE AES Society

- The most prevalent cause of bandwidth limitation in phased array radars is the use of phase shifters, rather than time delay devices, to steer the beam
 - Time shifting is not frequency dependent, but phase shifting is.

Adapted from Skolnik, Reference 1 IEEE New Hampshire Section IEEE AES Society

- With phase shifters, peak is scanned to the desired angle only at center frequency
- Since radar signal has finite bandwidth, antenna beamwidth broadens as beam is scanned off broadside
- For wide scan angles (60 degrees):
 - Bandwidth (%) ≈ 2 x Beamwidth (3 db half power) (deg)

- **Attributes of Thinned Arrays**
 - Gain is calculated using the actual number of elements

 $\mathbf{G} = \pi \mathbf{N}$

- Beamwidth equivalent to filled array
- Sidelobe level is raised in proportion to number of elements deleted
- Element pattern same as that with filled array, if missing elements replaced with matched loads

Example – Randomly Thinned Array

4000 Element Grid with 900 Elements

- These days, Taylor weighting is the most commonly used illumination function for phased array radars
 - Many other illumination functions can be used and are discussed in "Antennas-Part 1"
- Low sidelobe windows are often used to suppress grating lobes
- Amplitude and phase errors limit the attainable level of sidelobe suppression
- Phased array monopulse issues will be discussed in Parameter Estimation
 Adapted from Mailloux Reference 6

Adapted from Mailloux, Reference 6 IEEE New Hampshire Section IEEE AES Society

The Effect on Gain and Sidelobes of These Different Phenomena Can Usually Be Calculated

- Random errors in amplitude and phase in element current
- Missing or broken elements
- Phase shifter quantization errors
- Mutual Coupling effects

Adapted from Hsiao in Skolnik, Reference 1 IEEE New Hampshire Section IEEE AES Society

- Introduction
- Antenna Fundamentals
- Reflector Antennas Mechanical Scanning
- Phased Array Antennas
 - Linear and planar arrays
 - Grating lobes
 - Phase shifters and array feeds
 - Array feed architectures
- Frequency Scanning of Antennas
- Hybrid Methods of Scanning
- Other Topics

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Triangular Grid of Elements

$$\text{Lobes}\left(p,q\right)\text{at} \begin{cases} \mathbf{u}_{p} = \mathbf{u}_{o} + p\frac{\lambda}{\mathbf{d}_{x}}\\\\ \mathbf{v}_{q} = \mathbf{v}_{o} + q\frac{\lambda}{\mathbf{d}_{y}} \end{cases}$$

- Triangular grid used most often because the number of elements needed is about 14 % less than with square grid
 - Exact percentage savings depends on scan requirements of the array
 - There are no grating lobes for scan angles less than 60 degrees
- For a rectangular grid, and half wavelength spacing, no grating lobes are visible for all scan angles

ullet

BMEWS Radar, Fylingdales, UK

Courtesy of spliced (GNU)

Photo from Bottom of Array Face

Courtesy of Eli Brookner Used with Permission

Do All of these Phased Array Elements Transmit and Receive without Influencing Each Other ?

COBRA DANE Radar Shemya, Alaska

Courtesy of National Archives

Close-up Image Array Face

Courtesy of Raytheon Used with Permission

Do All of these Phased Array Elements Transmit and Receive without Influencing Each Other ?

- Analysis of Phased Arrays based on simple model
 No interaction between radiating elements
- "Mutual coupling" is the effect of one antenna element on another
 - Current in one element depends on amplitude and phase of current in neighboring elements; as well as current in the element under consideration
- When the antenna is scanned from broadside, mutual coupling can cause a change in antenna gain, beam shape, side lobe level, and radiation impedance
- Mutual coupling can cause "scan blindness"

Adapted from J. Allen, "Mutual Coupling in Phased Arrays" MIT LL TR-424 In addition ... mutual coupling can sometimes be exploited

to achieve certain performance requirements

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- If the phase of each element of an array antenna can be rapidly changed, then, so can the pointing direction of the antenna beam
 - Modern phase shifters can change their phase in the order of a few microseconds !
 - This development has had a revolutionary impact on military radar development
 - Ability to, simultaneously, detect and track, large numbers of high velocity targets
 - Since then, the main issue has been the relatively high cost of these phased array radars

The "quest" for \$100 T/R (transmit/receive) module

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TRADEX Radar Patriot Radar MPQ-53

Time to move beam ~20° order of magnitude seconds Time to move beam ~20° order of magnitude microseconds

Courtesy of NATO IEEE New Hampshire Section IEEE AES Society

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- The phase shift, ϕ , experienced by an electromagnetic wave is given by:

$$\phi = 2 \pi f L / v = 2 \pi f L \sqrt{\mu \epsilon}$$

- f = frequency, L = path length v = velocity of electromagnetic wave
- Note: v depends on the permeability, μ , and the dielectric constant, ϵ
- Modern phase shifters implement phase change in microwave array radars, mainly, by two methods:
 - Changing the path length (Diode phase shifters)
 Semiconductors are good switching devices
 - Changing the permeability along the waves path (Ferrite phase shifters)

EM wave interacts with ferrite's electrons to produce a change in ferrite's permeability

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Radiating Elements for Phased Array Antennas

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- How is the microwave power generated and distributed to the antenna elements?
- Passive vs. Active Array
 - Passive Array A single (or a few) transmitter (s) from which high power is distributed to the individual array elements
 - Active Array Each array element has its own transmitter / receiver (T/R) module

T/R modules will be discussed in more detail in lecture 18

- Constrained vs. Space Feed
 - Constrained Feed Array
 - Space Fed Array

- Concepts for feeding an array antenna :
 - Constrained Feed

Uses waveguide or other microwave transmission lines Convenient method for 2-D scan is frequency scan in 1 dimension and phase shifters in the other (more detail later)

- Space Feed

Distributes energy to a lens array or a reflectarray Generally less expensive than constrained feed no transmission line feed network Not able to radiate very high power

- Use of Subarrays

The antenna array may be divided into a number of subarrays to facilitate the division of power/ receive signal to (and from) the antenna elements

The AEGIS radar's array antenna utilizes 32 transmit and 68 receive subarrays

Phased Array Antenna Configurations (Active and Passive)

Adapted from Skolnik, Reference 1

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UHF Early Warning Radar

THAAD X-Band Phased Array Radar

Counter Battery Radar (COBRA)

APG-81 Radar for F-35 Fighter

S- Band AEGIS Radar

L- Band COBRA DANE Radar

Space Fed Arrays

Reflectarrays and Lens Arrays

MPQ-39 Multiple Object Tracking Radar (MOTR)

MOTR Space Fed Lens Antenna

8192 phase shifters (in a plane) take the place of the dielectric lens. The spherical wave of microwave radiation is phase shifted appropriately to form a beam and point it in the desired direction

Patriot Radar MPQ-53

S-300 "30N6E" X-Band Fire Control Radar*

* NATO designation "Flap Lid" – SA-10
Radar is component of Russian S-300 Air Defense System

Example of Space Fed - Reflectarray Antenna

S-300 "64N6E" S-Band Surveillance Radar*

Radar System and Transporter

- Radar system has two reflectarray antennas in a "back-to-back" configuration.
- The antenna rotates mechanically in azimuth; and scans electronically in azimuth and elevation

Radar Antenna

• * NATO designation "Big Bird" – SA-12

• Radar is component of Russian S-300 Air Defense System

Two Examples of Constrained Feeds (Parallel and Series)

Parallel (Corporate) Feed

End Fed - Series Feed

- Parallel (Corporate) Feed
 - A cascade of power splitters, in parallel, are used to create a tree like structure
 - A separate control signal is needed for each phase shifter in the parallel feed design
- Series Feed
 - For end fed series feeds, the position of the beam will vary with frequency
 - The center series fed feed does not have this problem
 - Since phase shifts are the same in the series feed arraignment, only one control signal is needed to steer the beam
- Insertion losses with the series fed design are less than those with the parallel feed

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- Beam steering in one dimension has been implemented by changing frequency of radar
- For beam excursion $\pm \theta_1$, wavelength change is given by:

$$\Delta \lambda = 2\lambda_{o} (\mathbf{D} / \mathbf{L}) \sin \theta_{1}$$

• If θ_1 = 45°, 30% bandwidth required for D/L = 5, 7% for D/L = 20

Adapted from Skolnik, Reference 1

Planar Array Frequency Scan Antenna

- The above folded waveguide feed is known as a snake feed or serpentine feed.
- This configuration has been used to scan a pencil beam in elevation, with mechanical rotation providing the azimuth scan.
- The frequency scan technique is well suited to scanning a beam or a number of beams in a single angle coordinate.

Adapted from Skolnik, Reference 1

SPS-48E

Courtesy of ITT Corporation Used with Permission

SPS-52

Courtesy of US Navy

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- Introduction
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- Frequency Scanning of Antennas
- Example of Hybrid Method of Scanning
 - Other Topics

ARSR-4 Antenna

Courtesy of Frank Sanders Used with Permission

ARSR-4 Array Feed

- Joint US Air Force / FAA long range L-Band surveillance radar with stressing requirements
 - Target height measurement capability
 - Low azimuth sidelobes (-35 dB peak)
 - All weather capability (Linear and Circular Polarization)
- Antenna design process enabled with significant use of CAD and ray tracing

- Phased arrays provide beam agility and flexibility
 - Effective radar resource management (multi-function capability)
 - Near simultaneous tracks over wide field of view
 - Ability to perform adaptive pattern control
- Phased arrays are significantly more expensive than reflectors for same power-aperture
 - Need for 360 deg coverage may require 3 or 4 filled array faces
 - Larger component costs
 - Longer design time
- Hybrid Antennas Often an excellent compromise solution
 - ARSR-4 is a good example array technology with lower cost reflector technology
 - ~ 2 to 1 cost advantage over planar array, while providing very low azimuth sidelobes

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Printed Antennas

Circular Patch Array in Anechoic Chamber

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Log - Periodic Antenna

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- Servomechanisms are used to control the angular position of radar antennas so as to compensate automatically for changes in angular position of the vehicle carrying the antenna
- Stabilization requires the use of gyroscopes, GPS, or a combination, to measure the position of the antenna relative to its "earth" level position
- Radars which scan electronically can compensate for platform motion by appropriately altering the beam steering commands in the radar's computer system

- Sheltering structure used to protect radar antennas from adverse weather conditions
 - Wind, rain, salt spray
- Metal space frame techniques often used for large antennas
 - Typical loss 0.5 dB
- Inflatable radomes also used
 - Less loss, more maintenance, flexing in wind

ALCOR

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MMW

- Enabling technologies for Phased Array radar development
 - Ferrite phase shifters (switching times ~ few microseconds)
 - Low cost MMIC T/R modules
- Attributes of Phased Array Radars
 - Inertia-less, rapid, beam steering
 - Multiple Independent beams
 - Adaptive processing
 - Time shared multi-function capability
 - Significantly higher cost than other alternatives
- Often, other antenna technologies can offer cost effective alternatives to more costly active phased array designs
 - Lens or reflect arrays
 - Reflectors with small array feeds, etc.
 - Mechanically rotated frequency scanned arrays

- Dr. Pamela R. Evans
- Dr. Alan J. Fenn

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- Skolnik, Reference 1
 - 9.11, 9.13, 9.14, 9.15, 9.18, and 9.34
 - For extra credit Problem 9.40